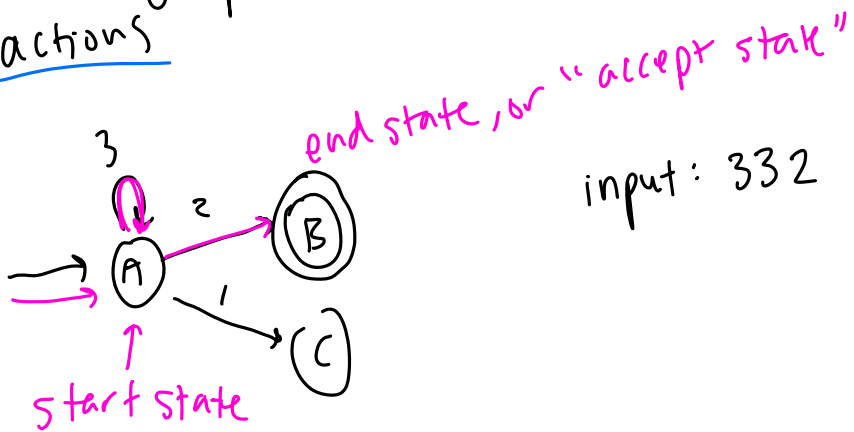
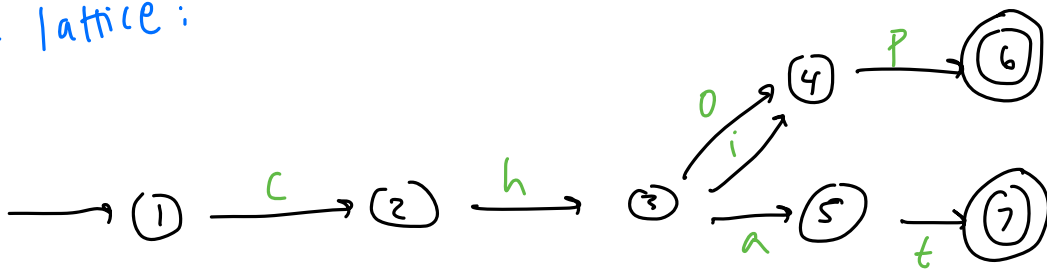


# State diagrams

directed graph where nodes are states and edges are actions



phone lattice:



chop, chip, chat are accepted.

State diagram is defined by

- Set of states  $S$
- Set of actions  $A$
- transition function  $\delta : S \times A \rightarrow \mathbb{P}(S)$

$$S = \{1, 2, 3, 4, 5, 6, 7\}$$

$$A = \{\text{english alphabet lowercase}\}$$

$$\delta(1, c) = \{2\}$$

$$\delta(3, o) = \{4\}$$

$$\delta(3, i) = \{4\}$$

⋮

$$\delta(1, i) = ? \quad \emptyset \text{ or } \{1\}$$

depends on question

In this class, only deterministic state machines:  $\delta : S \times A \rightarrow S$

example: build a deterministic state diagram that takes a sequence of 1,2,3's and enters an <sup>accept</sup> end state whenever the sum thus far is a multiple of 3.

input: 123 <sup>accept</sup>  
 1232 <sup>accept</sup> <sup>not accept</sup>

$$A = \{1, 2, 3\}$$

$$S = \{ \text{end state} \\ \text{mult. 3} \}$$

